

## Benefits

Linearization is an important tool in understanding the system behavior of a nonlinear system in a given state.

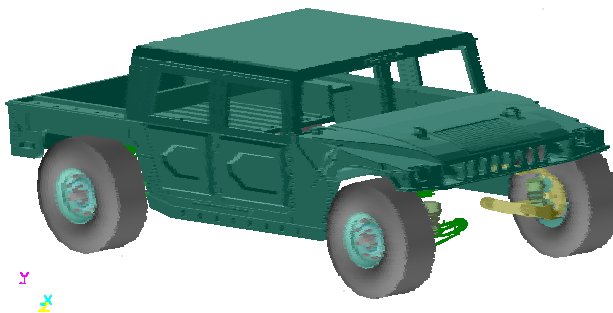
### Vibration Analysis at a System Level

- RecurDyn/Linear performs a linearization of the nonlinear RecurDyn model at a given operating state to prepare for an eigenvalue Analysis.
- The natural frequencies (eigenvalues) and mode shapes (eigenmodes) for the system model are calculated.
- System-level effects include interaction between components of an assembly and their constraints

### Support of Control System Design

- A linear plant model can provide the eigenvalues of the linearized equations of motion that are useful in verifying control logic and stability
- The linearized model can also be output in the form of state space matrices ( A, B, C and D state matrices) and state variables.
- Linearization of a constrained system includes the effect of algebraic constraint equations and corresponding Lagrange multipliers.

### • Eigenvalues of Humvee Model



#### Natural Frequencies

4th	1.13 Hz
5th	9.22 Hz
6th	13.11 Hz
7th	13.11 Hz
8th	13.82 Hz
9th	13.82 Hz
	:
	:

### • Eigenvectors of Connecting-Rod

#### 1<sup>ST</sup> MODE



Frequency 55.69 Hz

#### 2<sup>ND</sup> MODE

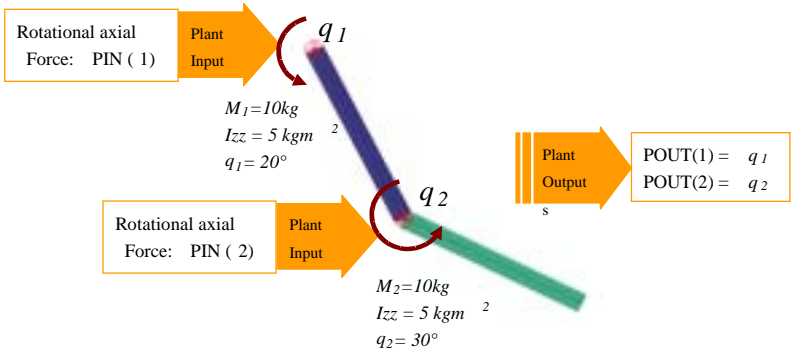


Frequency 73.15 Hz

## Generation of State Space Matrices

- State matrices can be directly imported into control system design packages.
- A state space representation gives the frequency response of the mechanical system
- The ability of feedback controllers to control and observe the model can be verified.

### Example: Double pendulum with 2 D.O.F.



#### STATE VARIABLES

	Name	Direction	Sign
1	RevJoint1	Velocity of ROTATION Z	-
2	RevJoint1	Displacement of ROTATION Z	-
3	RevJoint2	Velocity of ROTATION Z	-
4	RevJoint2	Displacement of ROTATION Z	-

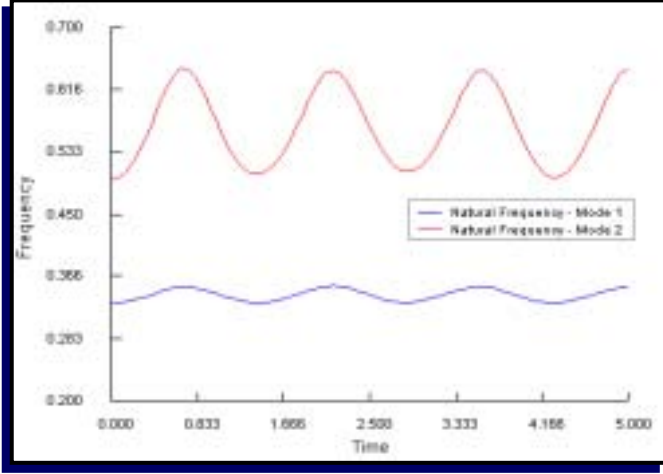
#### STATE MATRICES

	1	2	3	4
1	0.00026	-8.00210	0.00017	0.74566
2	1.00000	0.00000	0.00000	0.00000
3	-0.00075	8.41975	-0.00026	-6.01465
4	0.00000	0.00000	1.00000	0.00000

	1	2
1	0.06667	-0.10516
2	0.00000	0.00000
3	-0.10516	0.29920
4	0.00000	0.00000

	1	2	3	4
1	0.00000	1.00000	0.00000	0.00000
2	0.00000	0.00000	0.00000	1.00000

	1	2
1	0.00000	0.00000
2	0.00000	0.00000



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